University of Bahrain
College of Information technology
Department of Computer Engineering

Test (1)

Student Name	
I.D. No.	Solution
Section	

Course Title: Digital Logic
Course number: ITCE 202/250
Semester: 1
Academic Year: 2013/2014
Duration : 1hour
Date: 29/10/2013

Read the following before you start:
1. Write your name, ID and section number
2. Answer all questions.
3. Write your answers on the attached sheets only.

Question	Mark	Mark attained
1	22	
2	16	
3	15	
4	22	
5	25	
Total	100	

Question [1]: [22 mark]

(a) Convert the following numbers showing all steps.

3 $(1111)_2 = (\quad)_{BCD}$ $15_{10} = 0001\ 0101_{BCD}$

3 $(A29)_{16} = (\quad)_4$ $1010\ 0010\ 1001$ $2\ 2\ 0\ 2\ 2\ 1_4$

3 $(15)_{10} = (\quad)_{excess\_3}$ $0001\ 0101_{BCD} \xrightarrow{+3} 0100\ 1000_{excess\text{-}3}$

3 $(-35)_{10} = (\quad)_{1's\ complement}$

	64	32	16	8	4	2	1
Binary +35	0	1	0	0	0	1	1
1's Comp −35	1	0	1	1	1	0	0

(b) Add the following numbers in BCD

5 **$(97)_{10}+(25)_{10}=$**

$1001\ 0111$ 97
$0010\ 0101$ 25
$1011\ 1100$ 122
$0110\ 0110$
$0001\ 0010\ 0010$

5 **b)** Perform the following operation using 6-bit 2's complement numbers and indicate the case of an overflow.
$(-20)_{10}+(-15)_{10}=$

	32	16	8	4	2	1
+20	0	1	0	1	0	0
+15	0	0	1	1	1	1

-20 101100
-15 110001 +
-35 $\boxed{1}011101$
C = 1
V = 1

Question [2]: [16 mark]

1. Simplify the following expression using the Boolean algebra to a minimum number of literals:

8

$$\overline{A+B}+ABC+A\bar{B}$$

$\bar{A}\bar{B} + ABC + A\bar{B}$

$\bar{B}(\bar{A}+A) + ABC$

$\bar{B} + ABC$

$\bar{B} + AC$

2- Find the minimum Product of Sum for the following function, use Boolean Algebra.

8

$(a+b)(a+b+d)(a+c)$

$\bar{F} = \bar{a}\bar{b} + \bar{a}\bar{b}\bar{d} + \bar{a}\bar{c}$

$= \bar{a}\bar{b}(1+\bar{d}) + \bar{a}\bar{c}$

$= \bar{a}\bar{b} + \bar{a}\bar{c}$

$F = (a+b)(a+c)$

cd \ ab	00	01	11	10
00	0	0		
01	0	0		
11	0			
10	0			

$\bar{F} = \bar{a}\bar{b} + \bar{a}\bar{c}$

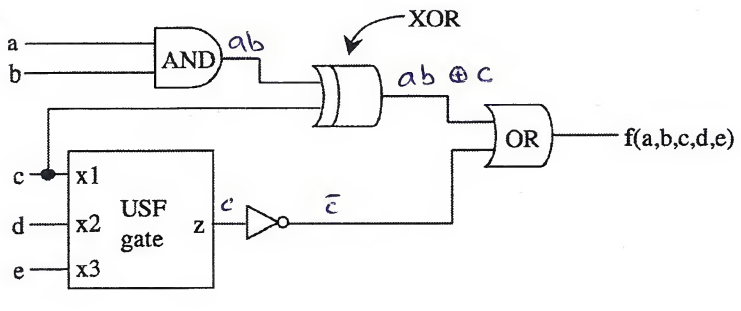
or use $x \cdot x + y = x$ Theorem 10 D on Page 52 to get $(a+b)(a+b+d)(a+c)$

$\Rightarrow (a+b)(a+c)$

Question [3]: [15 mark]

In the given circuit below, the gate labeled "USF gate" has the truth table shown below.

x1	x2	x3	z
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1



Write f(a,b,c,d,e) as a minimum sum of product.

(3) $Z = c$

(5) $f = (ab \oplus c) + \bar{c}$

(7)
$= ab\bar{c} + \bar{a}bc + \bar{c}$

$= ab\bar{c} + c(\bar{a} + \bar{b}) + \bar{c}$

$= ab\bar{c} + \bar{a}c + \bar{b}c + \bar{c}$

$= \bar{c}(ab + 1) + \bar{a}c + \bar{b}c$

$= \bar{c} + \bar{a}c + \bar{b}c$

$= \bar{c} + \bar{a} + \bar{b}c$

$= \bar{a} + \bar{b} + \bar{c}$

Question [4]: [22 mark]

a-- Find the maxterm expansion in algebrical expansion (in complete form) of the following expression:

8

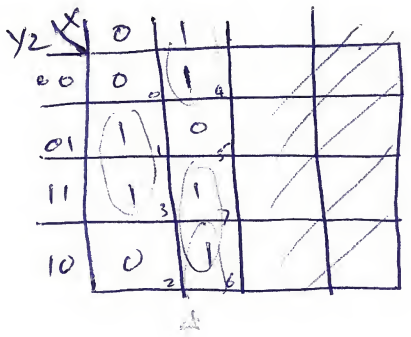
$$F(X,Y,Z) = XY + \bar{X}Z + X\bar{Y}\bar{Z}$$

$F = \Sigma m(1,3,4,6,7)$.

$= \Pi M(0,2,5)$

$\bar{F} = \bar{x}\bar{y}\bar{z} + \bar{x}y\bar{z} + x\bar{y}z$

$F = (x+y+z)(x+\bar{y}+z)(\bar{x}+y+\bar{z})$

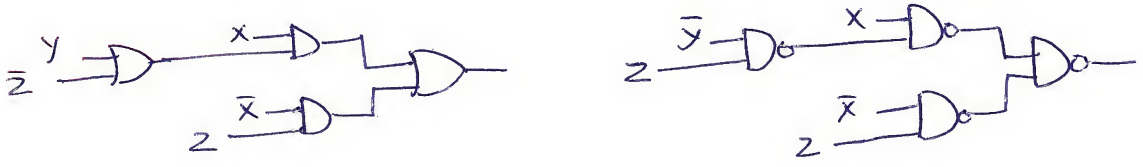


b-- Implement F using minimum 2-inputs NAND gates.

7

$F = XY + \bar{X}Z + X\bar{Z}$

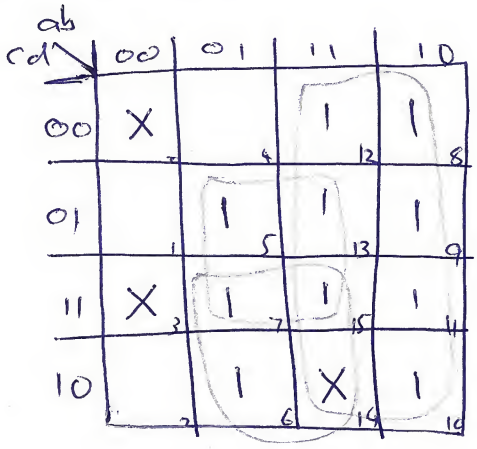
$= X(Y+\bar{Z}) + \bar{X}Z$



C -- Write **F(a,b,c,d) = Σm(5,6,7, 8,9,10,11, 12,13, 15) + Σd (0,3, 14)** as minimum sum of product.

7

$F = a + bd + bc$



Question [5]: [25 mark]

A combinational logic circuit receives BCD numbers as input. The output (W, X, Y, Z) represents the excess-3 code of the inputs. Consider the invalid inputs as don't care cases.

5 **(a)** Construct the truth table.
5 **(b)** Find the minterm expansion of W in decimal notation.
5 **(c)** Find the maxterm expansion of X in decimal notation.
5 **(d)**) Find the minimum SOP expression of Z.
5 **(e)** Implement Y using minimum number of NOR gates only.

(a)

	A B C D	W X Y Z
0	0 0 0 0	0 0 1 1
1	0 0 0 1	0 1 0 0
2	0 0 1 0	0 1 0 1
3	0 0 1 1	0 1 1 0
4	0 1 0 0	0 1 1 1
5	0 1 0 1	1 0 0 0
6	0 1 1 0	1 0 0 1
7	0 1 1 1	1 0 1 0
8	1 0 0 0	1 0 1 1
9	1 0 0 1	1 1 0 0
	1 0 1 0	x x x x
	1 0 1 1	x x x x
	1 1 0 0	x x x x
	1 1 0 1	x x x x
	1 1 1 0	x x x x
	1 1 1 1	x x x x

b) $W = \Sigma m(5, 6, 7, 8, 9) + \Sigma d(10, 11, 12, 13, 14, 15)$

c) $X = \Pi M(0, 5, 6, 7, 8) \cdot \Pi D(10, 11, 12, 13, 14, 15)$

d)

CD \ AB	00	01	11	10
00	1	1	X	1
01	0	0	X	0
11	0	0	X	X
10	1	1	X	X

$Z = \overline{D}$

e)

CD \ AB	00	01	11	10
00	1	1	X	1
01	0	0	X	0
11	1	1	X	X
10	0	0	X	X

$\overline{Y} = \overline{C}D + C\overline{D}$

$Y = (C + \overline{D})(\overline{C} + D)$